

Bayesian Methods: Multi-parameter Models -II

- Home Work discussion

Multinomial Models

- $p(y | \mathbf{q}) \propto \prod_1^k q_j^{y_j}, \sum q_j = 1, \sum y_j = n$
- likelihood involves powers of q_j 's
- Conjugate prior: same form
 - Dirichlet distribution $\text{Dir}(\mathbf{a}_1, \mathbf{a}_2, \dots, \mathbf{a}_k)$ (generalization of beta for two classes)
 - $\propto \prod q_j^{\mathbf{a}_j - 1}$
- Posterior: Dirichlet $\text{Dir}(\mathbf{a} + y)$
 - Improper ?, Uniform ?
 - Posterior proper if $\mathbf{a} + y > 0$
- Example: 3 or more categories on an item response survey
 - could make posterior inference on any function of \mathbf{q}

Multivariate Normal

- Known Covariance matrix Σ
 - Likelihood: quadratic form in mean vector
 - Conjugate Prior involves a quadratic form
 - Posterior updates the mean and covariance(precision) matrix
 - Marginals of subvectors
 - Predictive Distribution
 - Draw samples from Multivariate Distribution
 - Cholesky Decomposition
 - Principal Components
 - Non-informative prior
 - Proper posterior: needs $n > d$
 - Density does not exist if Cov matrix singular

- Unknown mean and Covariance
 - Conjugate: Normal-Inverted Wishart
 - Try the idea of independent components

Bioassay Problem

- Binomial, Logit