

An Associative Network Model for  
Advertising: A Hierarchical Bayesian  
Approach

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# Overview

- Advertising and background
- Marketing data
- Associative Network
- Proposed model
- Preliminary simulation & estimation procedure
- Assumptions
- Work in Progress
- Conclusions

# Advertising

- Marketing communicators spend millions on advertising, trying to influence consumers' brand-related beliefs and attitudes.
- Consumers' minds however, are black boxes.
- Innumerable models have been proposed that focus on different aspects of advertising effectiveness like cognition, feelings, product usage experience etc.
- Difficult to come up with one unified theory for advertising effectiveness.

# Models in Advertising

- Elaboration Likelihood Model (ELM): ***Petty & Cacioppo***
  - Individuals may form their attitudes in two ways (centrally or peripherally).
  - Under central processing, advertising messages are processed through counter-arguing and support arguing. Under peripheral processing individuals rely on cues such as celebrity status of the product endorser.
- Integrated Information Response model (IIRM): ***Smith & Swinyard***
  - Concept of “low order beliefs” -> “high order beliefs”.
- Conglomeration of advertising studies: ***Vakratsas & Ambler***
  - Look at a plethora of models in advertising.
  - Summarize different consumer advertising processing models.

# Marketing Data

Typical marketing data collected includes:

- Motivating Conditions
- Brand Attributes
- Brand Beliefs
- Consideration Sets

# Motivating Conditions for Tooth brushing

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## Solving Immediate Problems

- a1: My teeth stain easily.
- a2: I wake up with a bad taste/feeling in my mouth.
- a3: I am concerned about the condition of my gums
- a4: I am predisposed to having sensitive teeth.
- a5: I am concerned about tartar and plaque build-up on my teeth.
- a6: I am concerned about bad breath.
- a7: My teeth are dull/not white enough.
- a8: I am predisposed to having cavities.
- a9: I have trouble getting my kids to brush.
- a10: I am concerned about germs and mouth infections.

## Preventing Potential Problems:

- b1: I would feel I'm letting myself down if I didn't brush regularly.
- b2: I believe that people expect me to brush regularly

## Enjoying Sensory Pleasure:

- e1: I like the tingle I feel in my mouth after I brush.
- e2: I enjoy the fresh taste I get from brushing.
- e3: I love to see my teeth gleaming like pearls.
- e4: Bubbling action adds to the sensory pleasure of brushing.

## Displeasure in Use:

- f1: Toothpastes are too strong tasting.
- f2: Toothpastes scratch the enamel on my teeth.
- f3: Toothpastes irritate my mouth.
- f4: Toothpastes cost too much.
- f5: Toothpastes contain artificial ingredients.
- f6: Toothpaste packaging can be harmful to the environment.

# Example Question

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Person BJ	Person AW	Person MC	Person JD
Stains, bad taste/feel in my mouth and gums aren't a problem for me	My teeth stain easily.	I wake up with a bad taste/ feeling in my mouth.	I am concerned about the condition of my gums
Sensitive teeth, tartar, plaque and bad breath aren't a problem for me.	I am predisposed to having sensitive teeth.	I am concerned about tartar and plaque build-up on my teeth.	I am concerned about bad breath.
Regularly brushing my teeth doesn't figure in my self image, or the impression I want to create.	I would feel I'm letting myself down if I didn't brush regularly.	I believe that people expect me to brush regularly.	I believe that people expect me to brush regularly.

# Toothpaste Attributes/Benefits

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## Medical Benefits:

- A1: Helps prevent cavities.
- A2: Helps remove tartar and plaque.
- A3: Helps promote healthy gums.
- A4: Helps fight germs and infections in your mouth.

## Taste:

- B1: Mild tasting.
- B2: Fresh tasting.
- B3: Gives your mouth a tingle.
- B4: A taste kid's love.
- B5: Great bubbling action.

## Abrasiveness:

- C1: Doesn't irritate my mouth.
- C2: For sensitive teeth.

## Resulting Appearance:

- D1: Helps clean teeth.
- D2: Helps remove stains.
- D3: Whitens your teeth.

## Resulting Breath:

- E1: Fights bad breath.
- E2: Freshens breath for 12 hours.
- E3: Helps take away morning mouth.

## Price:

- F1: Regular price\*.
- F2: 20% less.

## Ingredients:

- G1: 80% natural /20% artificial ingredients\*.
- G2: 100% natural ingredients.

## Interests:

- I1: An interesting way to clean your teeth
- I2: Provides a change of pace

## Social:

- J1: Shows others you care about your teeth
- J2: Helps you feel good about yourself for brushing regularly



# Brand Beliefs \*\*

	<u>AQUAFRESH</u>	<u>COLGATE</u>	<u>CREST</u>	<u>MENTADENT</u>
1. Helps prevent cavities.....	_____	_____	_____	_____
2. Delivers protection in hard to reach places. ....	_____	_____	_____	_____
3. Helps remove tartar and plaque .....	_____	_____	_____	_____
4. Helps promote healthy gums.....	_____	_____	_____	_____
5. Penetrates to strengthen your teeth against cavities.....	_____	_____	_____	_____
6. Helps fight germs and infections in your mouth. ....	_____	_____	_____	_____
7. Mild tasting.....	_____	_____	_____	_____
8. Fresh tasting.....	_____	_____	_____	_____
9. Gives your mouth a tingle. ....	_____	_____	_____	_____
10. A taste kids love. ....	_____	_____	_____	_____

# Consideration set \*\*

When I buy toothpaste: *(Please mark only one box)*

- I usually buy the same toothpaste brand
- I usually buy one of the same two or three brands
- I keep trying different brands
- I buy toothpaste without noting what the brand is

When I buy toothpaste: *(Please mark only one box)*

- I usually buy a nationally advertised brand
- I usually buy a store brand
- I sometimes buy a nationally advertised brand, sometimes a store brand

When I buy toothpaste for myself, I:

- Buy a particular brand
- Do not buy a particular brand

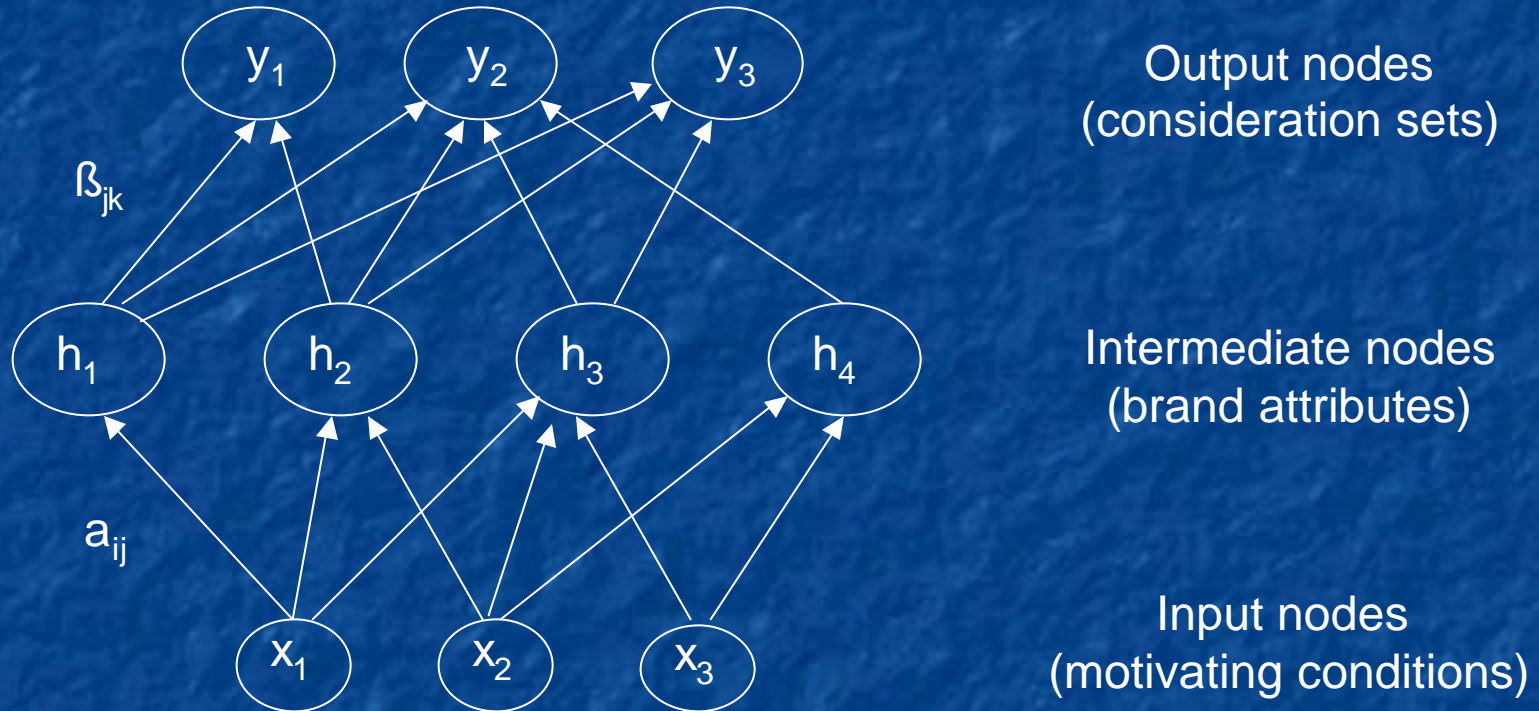
*(If Yes) Which brand? (Please mark only one box)*

- Aquafresh
- Colgate
- Crest
- Mentadent
- Other brand (please specify) \_\_\_\_\_

# Associative Networks

- Intended to represent abstract models of the brain
- Numerous computational units that are highly interconnected, called nodes and represent biological neurons.
- Similar to MLP Feedforward networks with single hidden layer.

# Associative Net Framework



# Associative Net Framework (Contd...)

$x$  → Motivating conditions

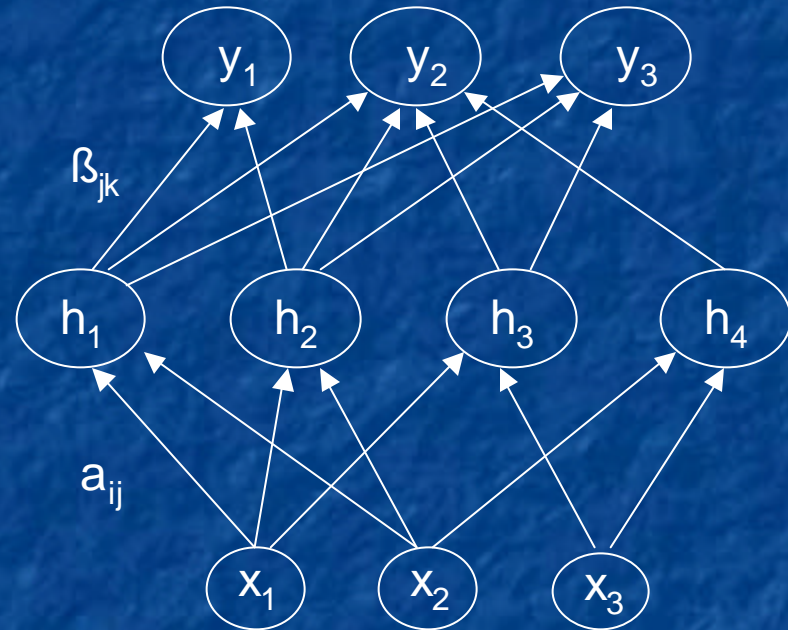
$\alpha$  → Attribute efficacy

$h$  → Attributes

$\beta$  → Brand belief

$y$  → Consideration set

$\theta$  → Threshold



# Hierarchical Model

$$x_T = 1 \text{ if } \mathbf{e}_i \geq \mathbf{q}_{x,y}$$

$$x_T = 0 \text{ if } \mathbf{e}_i < \mathbf{q}_{x,y}$$

$$h_j = 1 \text{ if } \sum_i x_i \mathbf{a}_{ij} \geq \mathbf{q}_h$$

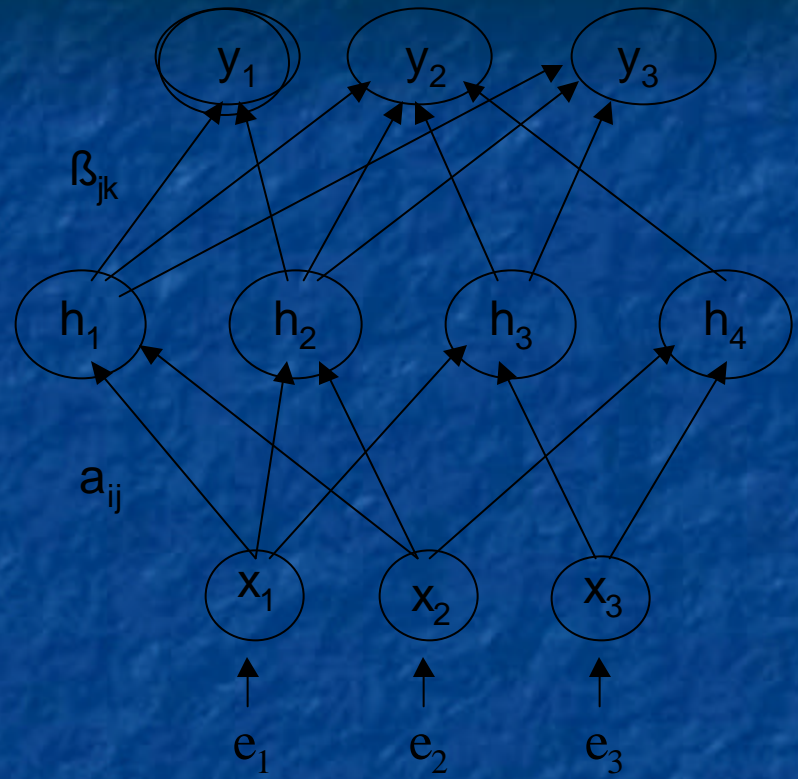
$$h_j = 0 \text{ if } \sum_i x_i \mathbf{a}_{ij} < \mathbf{q}_h$$

$$y_k = 1 \text{ if } \sum_j h_j \mathbf{b}_{jk} \geq \mathbf{q}_{x,y}$$

$$y_k = 0 \text{ if } \sum_j h_j \mathbf{b}_{jk} < \mathbf{q}_{x,y}$$

$$x_O = 1 \text{ if } \mathbf{e}_i \geq \mathbf{q}_{x,y} - \mathbf{d}$$

$$x_O = 0 \text{ if } \mathbf{e}_i < \mathbf{q}_{x,y} - \mathbf{d}$$



$$\mathbf{q}_h = \mathbf{g}_0 + \mathbf{g}^* (IS)$$

# Hierarchical Model

$$[y | \mathbf{q}_{x,y}, \mathbf{b}, h]$$

$$[h | \mathbf{q}_h, x_T, \mathbf{a}]$$

$$[\mathbf{q}_h | \mathbf{g}_0, \mathbf{g}, IS]$$

$$[x_T | \mathbf{e}, \mathbf{q}_{x,y}]$$

$$[x_O | \mathbf{e}, \mathbf{d}, \mathbf{q}_{x,y}]$$

$$[\mathbf{e}]$$

Hierarchy

Likelihood

$$[y | \mathbf{q}_{x,y}, \mathbf{b}, \mathbf{g}, IS, \mathbf{g}_0, x_T, \mathbf{e}, \mathbf{a}] [x_O | \mathbf{e}, \mathbf{d}, \mathbf{q}_{x,y}]$$

Conditional Independence

$$[y | \mathbf{q}_{x,y}, \mathbf{b}, \mathbf{g}, IS, \mathbf{g}_0, x_T, \mathbf{a}] [x_T | \mathbf{e}, \mathbf{q}_{x,y}] [x_O | \mathbf{e}, \mathbf{d}, \mathbf{q}_{x,y}] [\mathbf{e}] [\mathbf{q}_{x,y}] [\mathbf{q}_0] [\mathbf{g}] [\mathbf{d}] [\mathbf{a}] [\mathbf{b}]$$

# Preliminary Assumptions

We assume that we know:

$y \rightarrow$  consideration set (data)

$\alpha \rightarrow$  Attribute efficacy

$\beta \rightarrow$  Brand belief (data)

} Network structure known  
(initially)

We assume the same threshold ( $\theta$ ) for two layers in the network

Some of these assumptions will be relaxed (discussed in future work).



# Simulation

Data is simulated based on the network shown:

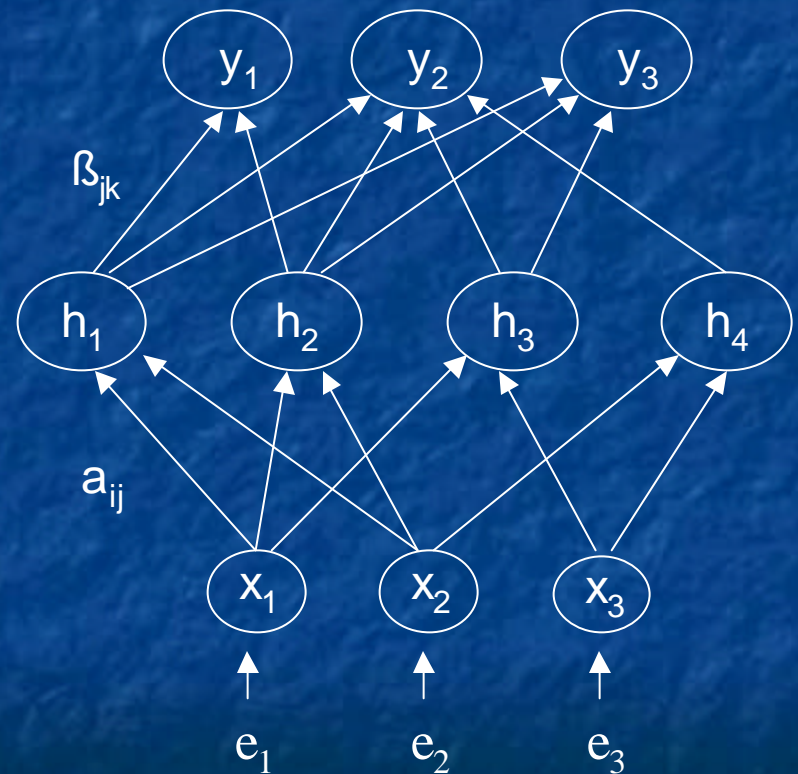
$$\text{With } \mathbf{a} = \begin{pmatrix} 0.33 & 0.33 & 0.33 & 0 \\ 0.33 & 0.33 & 0 & 0.33 \\ 0 & 0 & 0.5 & 0.5 \end{pmatrix}$$

$$\mathbf{\beta} = \begin{pmatrix} 0.33 & 0.33 & 0.33 \\ 0.33 & 0.33 & 0.33 \\ 0 & 0.5 & 0.5 \\ 0 & 1 & 0 \end{pmatrix}$$

$$? = 0.3$$

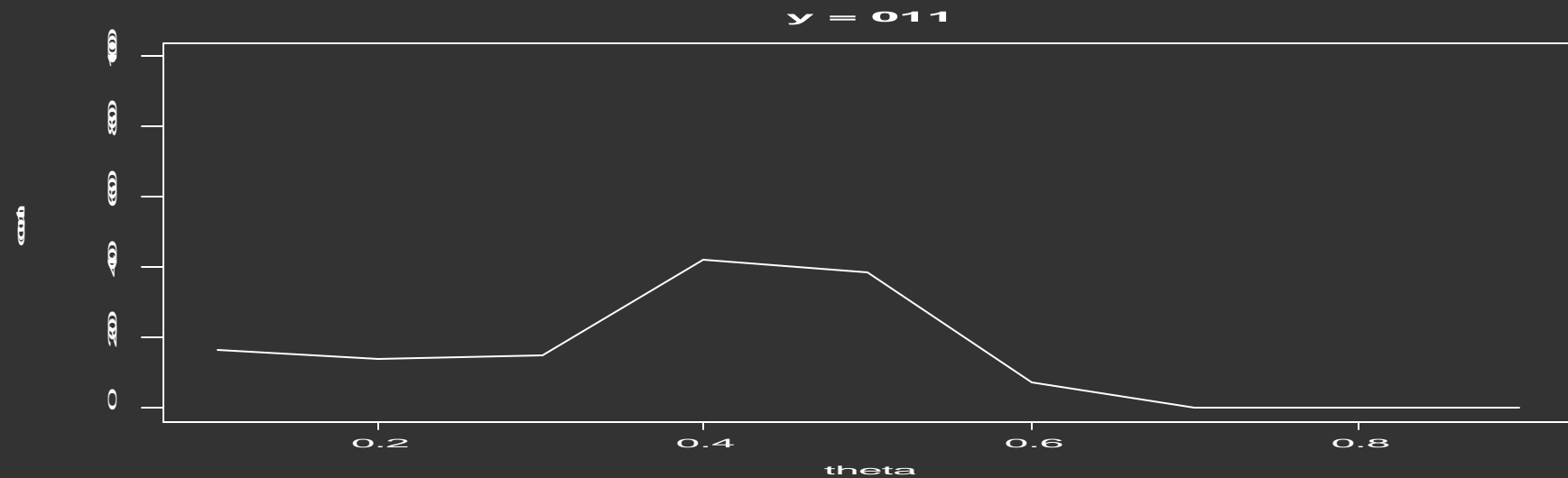
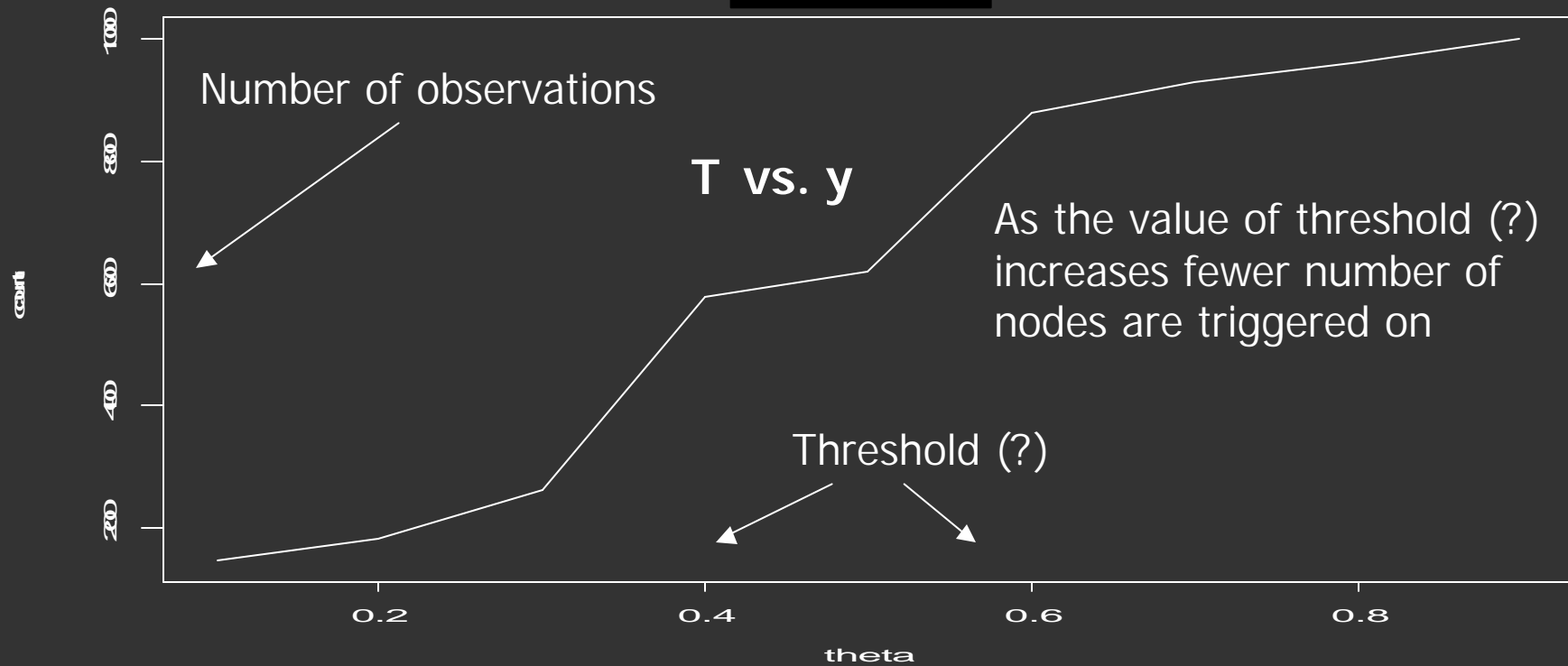
Draw  $e_{it}$ 's  $\sim$  i.i.d.  $N(0,1)$

Compute the  $y$ 's.



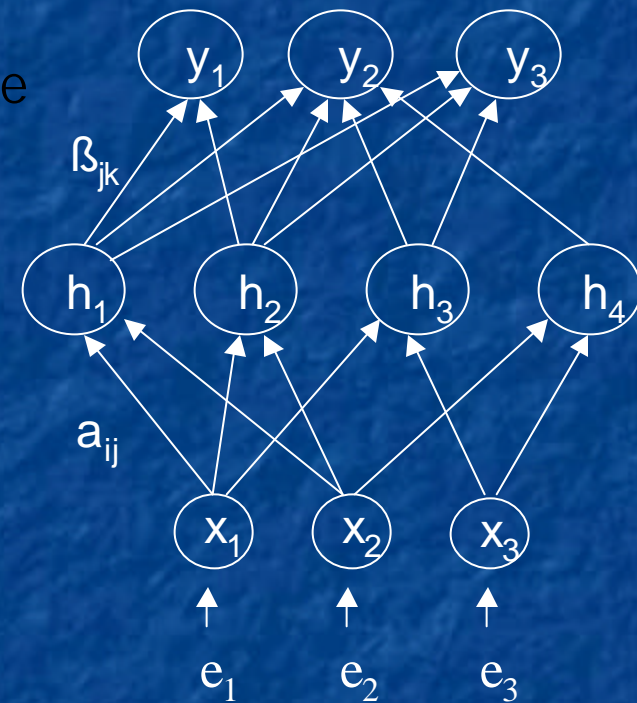
# Subset of the simulated data

$e_1$	$e_2$	$e_3$	$y_1$	$y_2$	$y_3$
0.31	-0.35	0.52	1	1	1
-1.2	-0.89	0.91	0	1	1
0.14	-1.14	0.01	1	1	1
-1.16	0.63	0.23	1	1	1
-0.89	0.35	-0.65	1	1	0
1.17	-0.31	-0.98	1	1	1
-0.38	-0.95	1.13	0	1	1
0.5	1.21	-0.62	1	1	1
0.54	1.22	-1.2	1	1	1
1.14	1.1	1.07	1	1	1
-1.58	1.08	0.56	1	1	1
0.71	-0.21	-0.58	1	1	1
0.15	-1.15	-2.95	1	1	1
0.99	-0.28	-1.58	1	1	1
-1.09	-0.09	-0.78	0	0	0
-0.71	-0.11	0.78	0	1	1
-0.01	-0.69	0.07	0	0	0
0.45	-0.81	1.42	1	1	1
-1.39	0.62	-1.43	1	1	0
0.95	-1.65	-0.26	1	1	1



# Preliminary Estimation Procedure

- Step 1:  $[\mathbf{e}_1 | \mathbf{e}_2, \mathbf{e}_3, \mathbf{q}, y]$ 
  - if  $e_1 > ? \Rightarrow x_T = 1$ , if  $e_1 < ? \Rightarrow x_T = 0$
  - Let  $x_T = 1$ , compute the  $y$ 's ( $y_{out}$ ) and compare  $y_{out}$  to  $y_{obs}$
  - if  $x_T = 1$  and  $y_{out} = y_{obs} \Rightarrow e_1 > ?$   
if  $x_T = 0 \Rightarrow e_1 < ?$   
else  $x_T = 1$  or  $0 \Rightarrow e_1 \sim$  Normal dist. with truncation at  $?-d$  (depending on  $X_0$ )
- Step 2:  $[\mathbf{e}_2 | \mathbf{e}_1, \mathbf{e}_3, \mathbf{q}, y]$ 
  - Draw  $e_1$  from the feasible region
  - Repeat step 1 to obtain feasible region for  $e_2$
- Step 3:  $[\mathbf{e}_3 | \mathbf{e}_1, \mathbf{e}_2, \mathbf{q}, y]$



# Estimation Procedure Contd...

$$p(\mathbf{e}_1 | \mathbf{e}_2, \mathbf{e}_3, \mathbf{q}, y) = \sum_{x_1} p(\mathbf{e}_1 | \mathbf{e}_2, \mathbf{e}_3, \mathbf{q}, x_1, y) \underbrace{p(x_1 | \mathbf{e}_2, \mathbf{e}_3, \mathbf{q}, y)}_{I[x_1 | \mathbf{e}_2, \mathbf{e}_3, \mathbf{q}, y]}$$

- Step 4:  $[\mathbf{q} | \mathbf{e}_1, \mathbf{e}_2, \mathbf{e}_3, y]$

$$\mathbf{q}^{(n)} = \mathbf{q}^{(o)} + eps$$

Random walk Metropolis-Hastings

$$eps \sim N(0, 0.01)$$

$$[\mathbf{q}] \sim Unif[-5, 5]$$

1 or 0, if matches the output  
accept new ? else reject

$$a = \min\left(\frac{\prod_i [y_i | \mathbf{q}^{(n)}, \mathbf{e}_i][\mathbf{q}^{(n)}]}{\prod_i [y_i | \mathbf{q}^{(o)}, \mathbf{e}_i][\mathbf{q}^{(o)}]}, 1\right)$$

Denominator evaluates to 1

- Repeat steps 1 through 4

# Work in progress

- Estimating the  $\alpha$ 's &  $\beta$ 's.
- Assume different  $\theta$ 's for different layers of the network.
- Find out the admissible values for starting off the Markov chain.
- Impose more constraints, consistent with theory, on  $\theta$ 's.

# Conclusion

- An attempt to use an associative net framework to explain how advertising works.
- Advertising can impact the attribute weights in a simple regression equation by linking needs to attributes that are responsive.
- Advertising can change the network structure.
- Tries to understand the impact of advertising from this new perspective